

# Lecture 7: Filters & Reverb

1. Filters & EQ
2. Time delay effects
3. Reverb

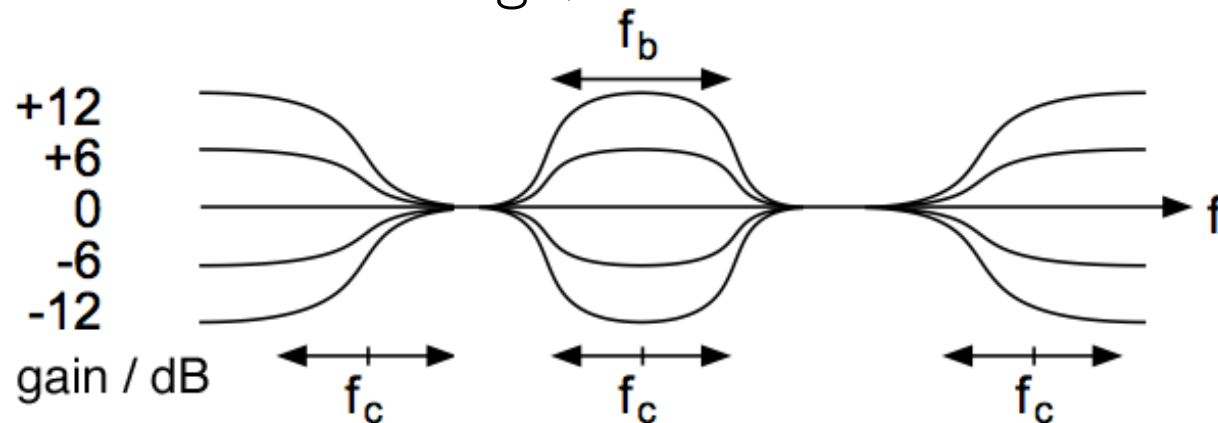
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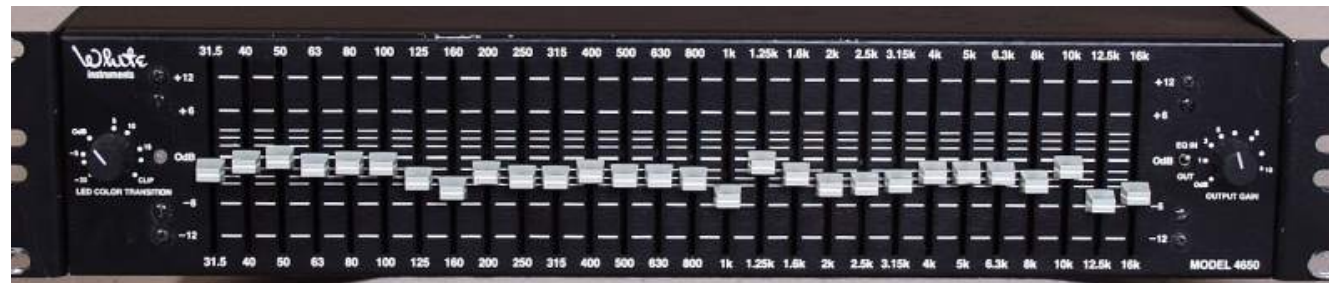
dpwe@ee.columbia.edu    <http://www.ee.columbia.edu/~dpwe/e4896/>

# I. Filters & EQ

- **EQ** is a critical tool in audio mixing
  - boost/cut on single control
  - each instrument has its own “space”
- Different **formats**
  - Low/Mid/High, Parametric



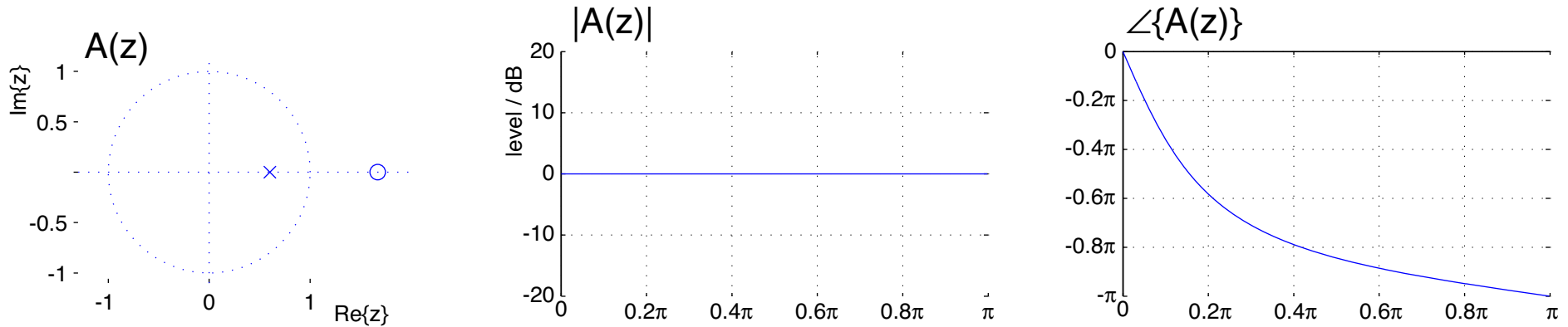
- Graphic EQ



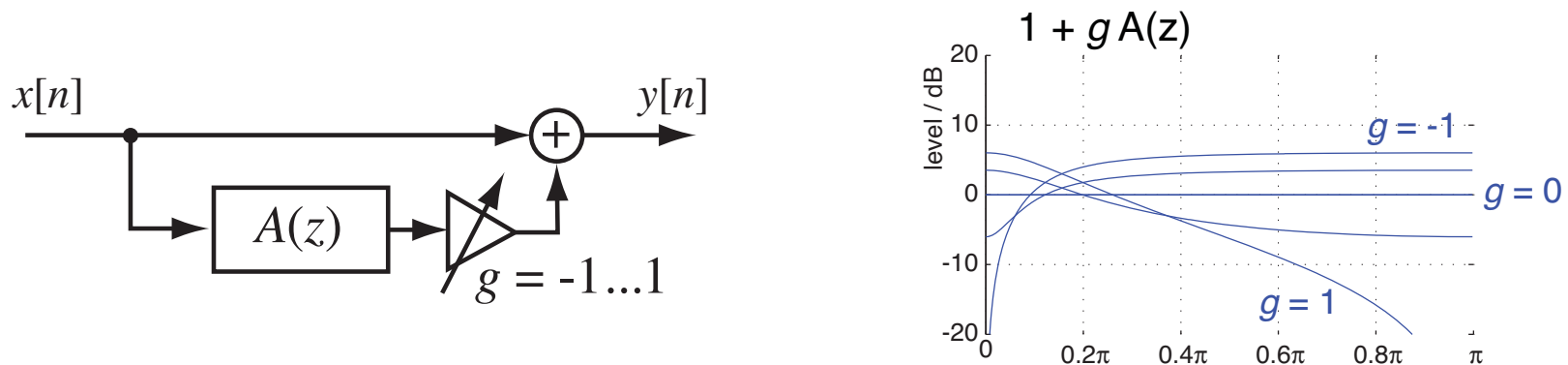
# EQ filters

- How to get **boost** + **cut** from a single filter?

- use **allpass**



- then +/- to get **phase** cancellation/reinforcement

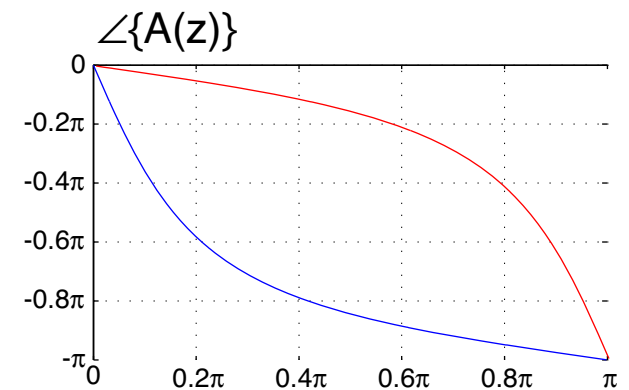
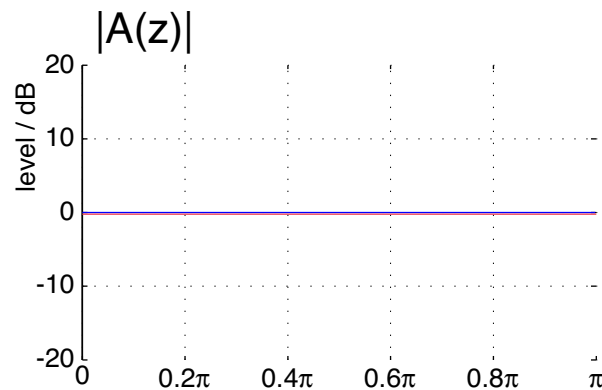
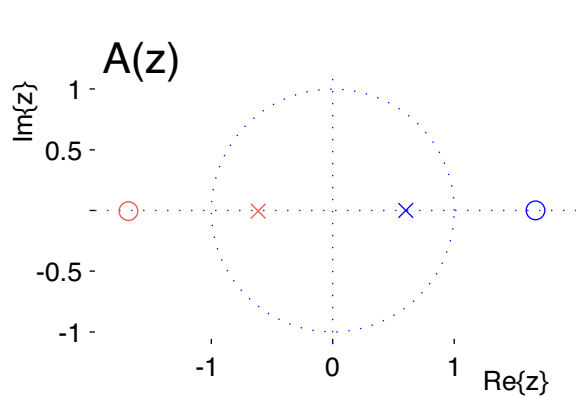


# Allpass Filters

- Allpass filters have **flat gain**:  $|A(e^{j\omega})| = 1$ 
  - from **mirror-image** numerator and denominator:

$$A(z) = \frac{z^{-m} D_m(z^{-1})}{D_m(z)}$$

- e.g. for  $D_m(z) = 1 - 0.6z^{-1} \Rightarrow A(z) = \frac{-0.6 + z^{-1}}{1 - 0.6z^{-1}}$



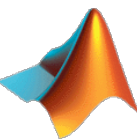
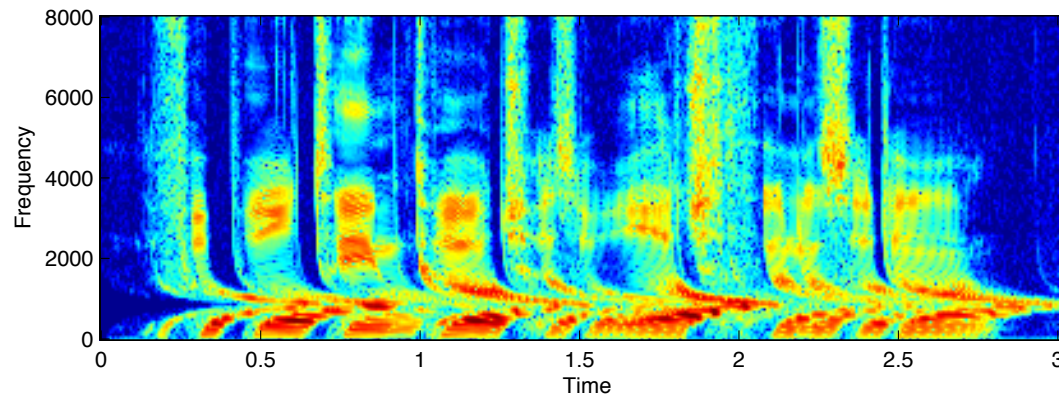
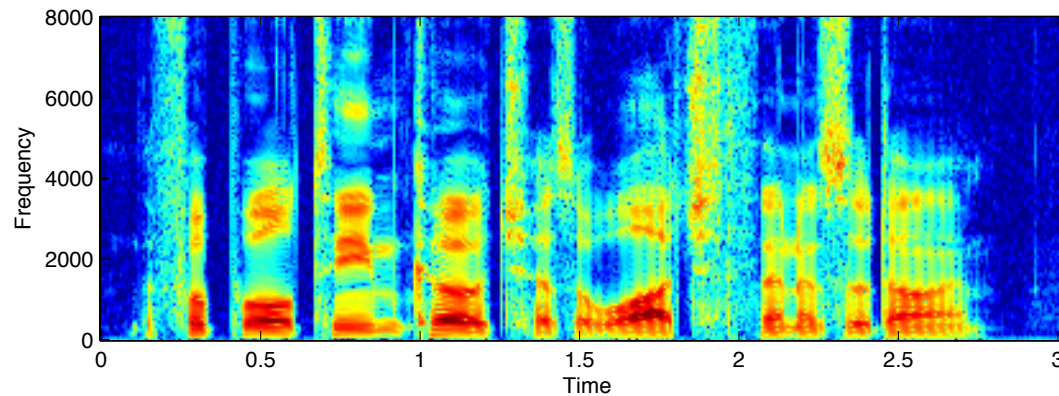
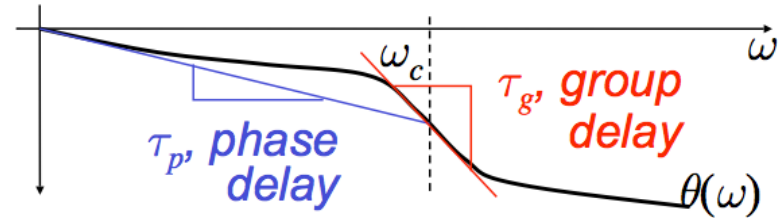
- slope governs **phase interactions**, **group delay**

$$\tau_g(\omega_c) = - \left. \frac{d\theta(\omega)}{d\omega} \right|_{\omega=\omega_c}$$

# Group Delay

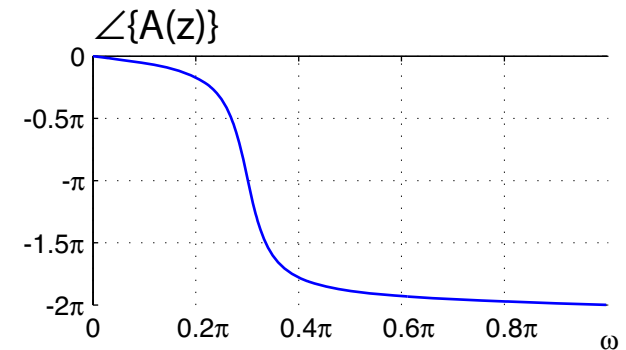
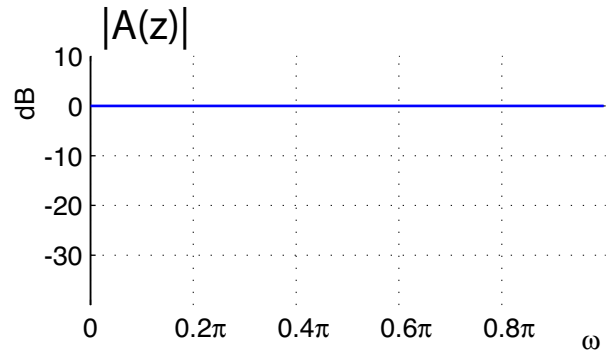
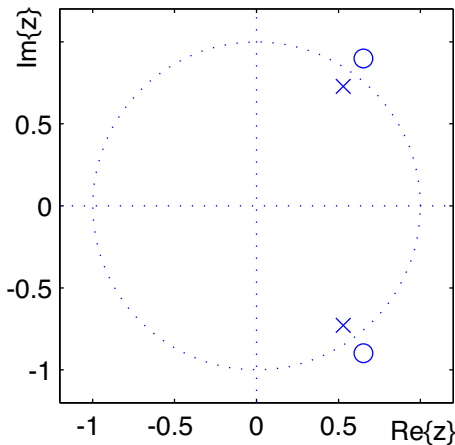
- Local phase change of  $H(z)$  governs effective delay of that frequency region: “group delay”

$$\tau_g(\omega_c) = - \left. \frac{d\theta(\omega)}{d\omega} \right|_{\omega=\omega_c}$$



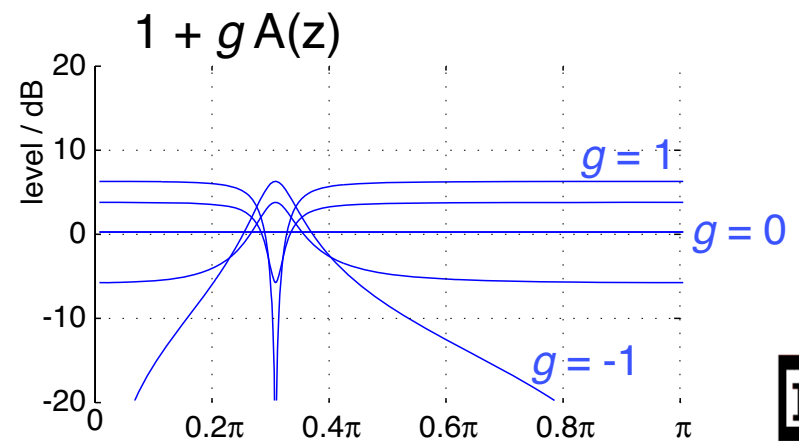
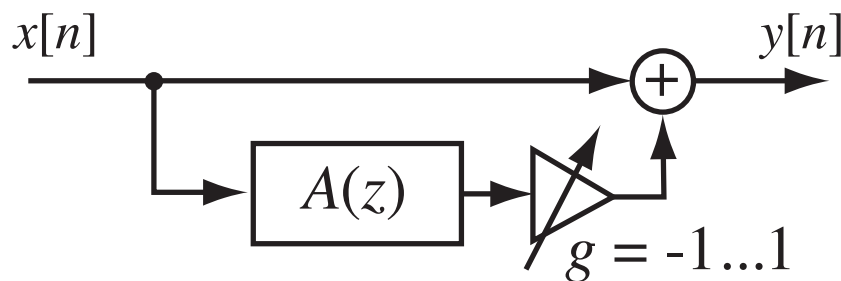
# Parametric EQ

- **2nd order Allpass** → **slope** & **place**  $\theta(\omega) = \pi$



- angle → frequency
- radius → slope → bandwidth

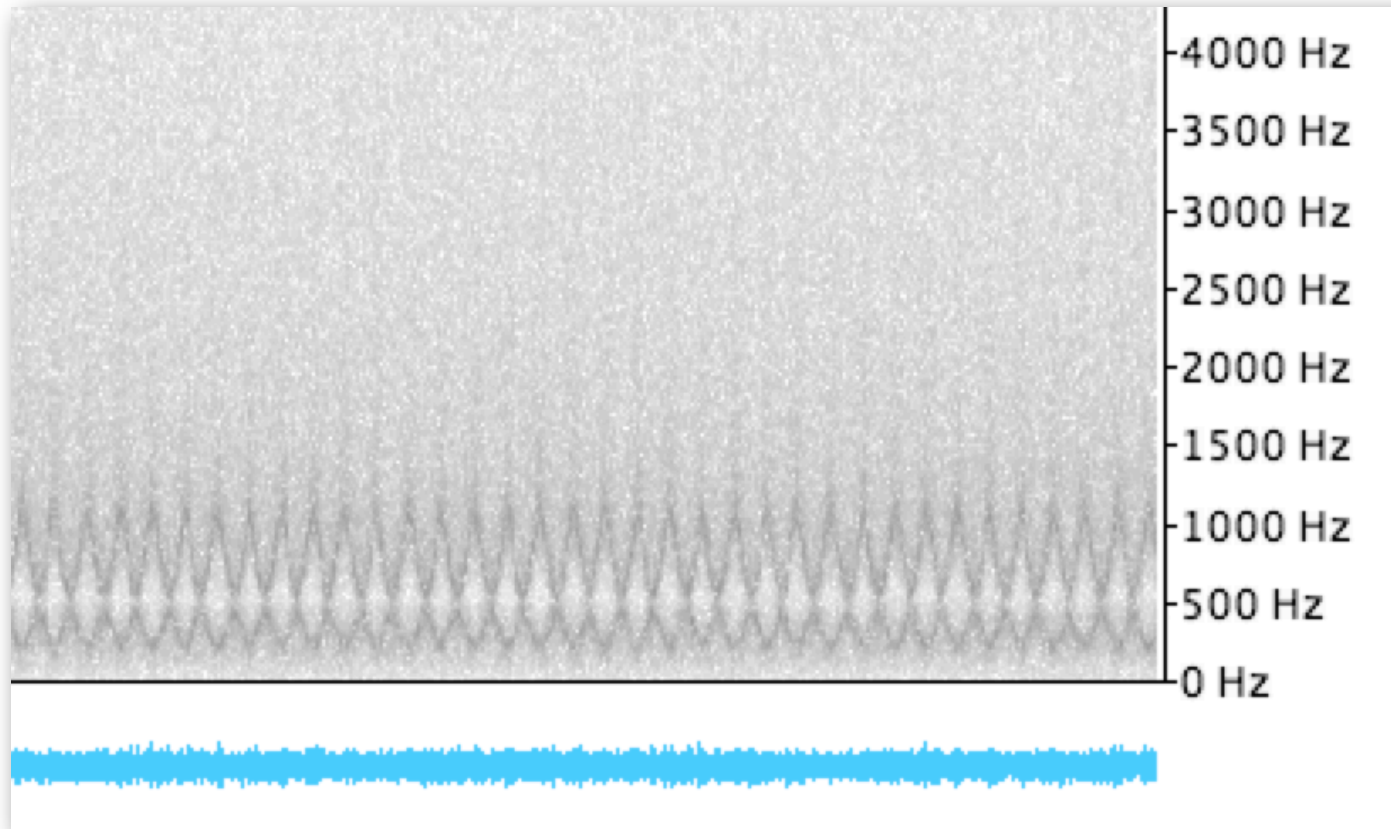
- Same structure for EQ





# Time-Varying Filters

- Classic Wah-Wah ?



- Iterated Filters...



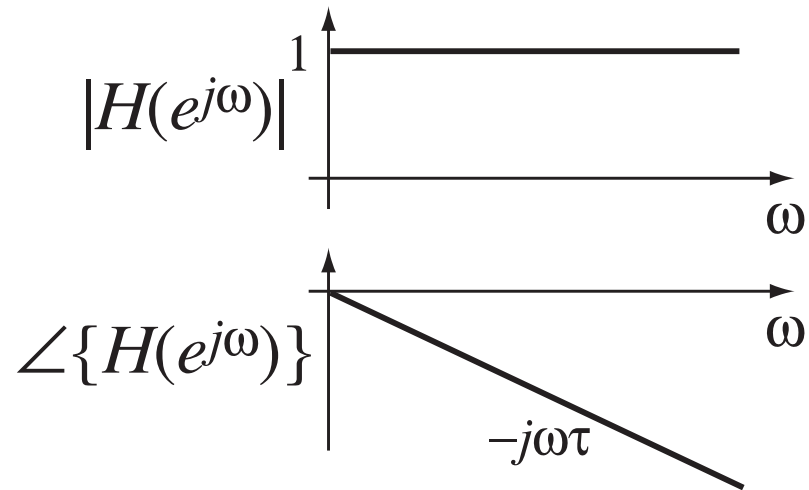
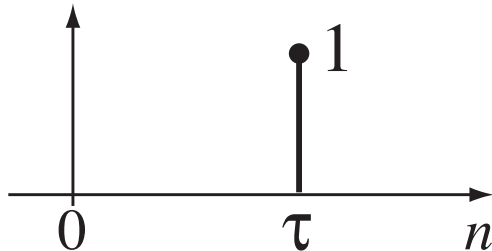
s07-wahwah.pd

# 2. Time Delays

- **Delays** correspond to **sound propagation**
  - 340 m/s  $\approx$  1 foot / ms
- **Delays** are a simple kind of **filter**
  - can analyze from **Fourier** perspective...



$$h[n] = \delta[n - \tau]$$
$$\Rightarrow H(e^{j\omega}) = e^{-j\omega\tau}$$

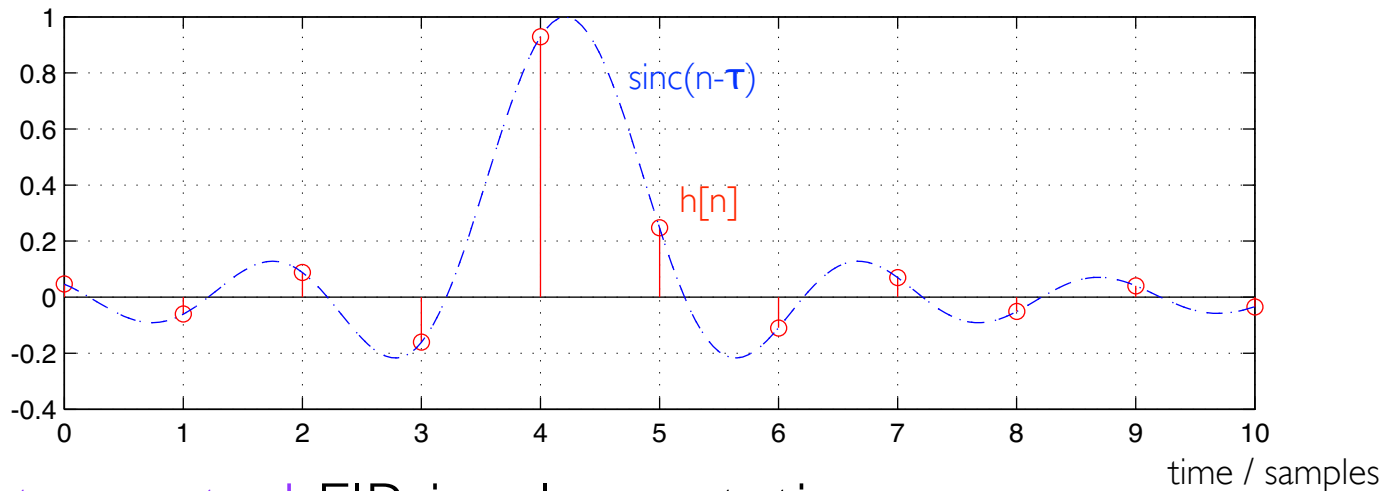




# Fractional Delays

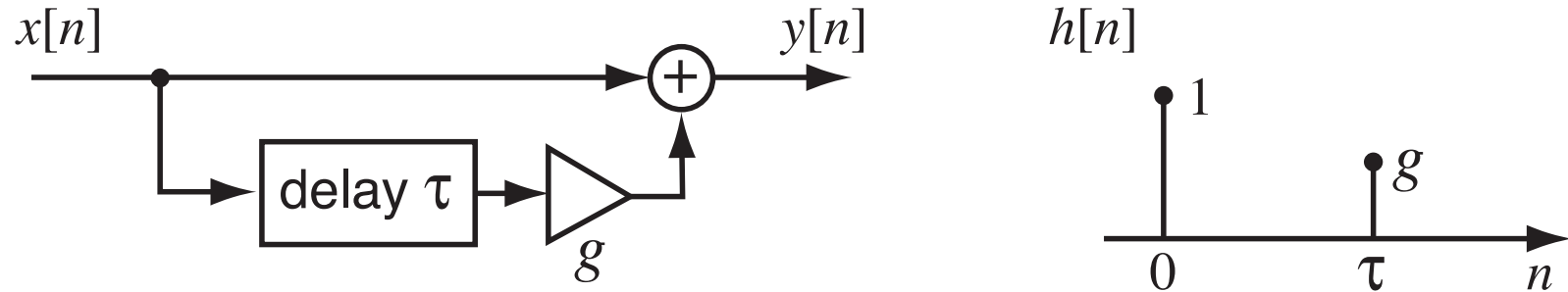
- For short delays, one sample **quantization** may be too coarse
  - 1 sample @ 44.1 kHz = 22.7  $\mu$ s
- **Fractional delay** can be recovered from Fourier domain

$$e^{-j\omega\tau} \Leftrightarrow \frac{\sin \pi(n - \tau)}{\pi(n - \tau)} = \text{sinc}(n - \tau)$$

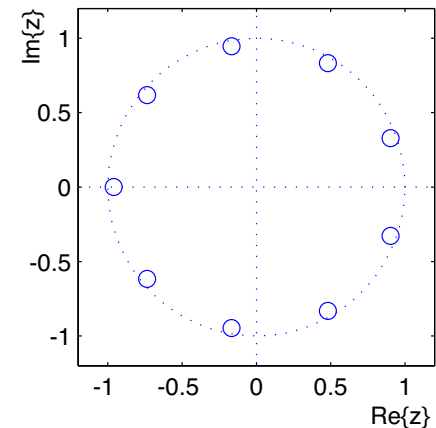
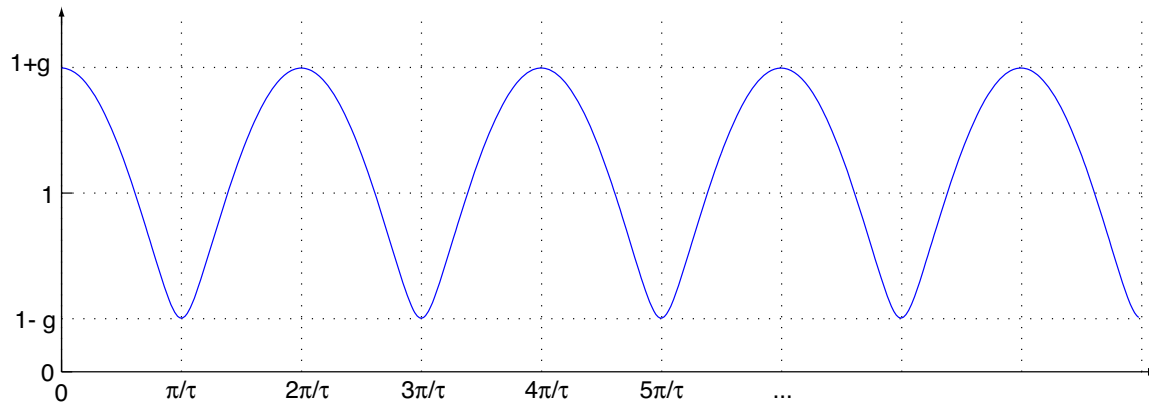


- truncated FIR implementation

# Comb Filters



- **Delay** added to **direct path** causes “**comb**”
  - .. from phase interactions

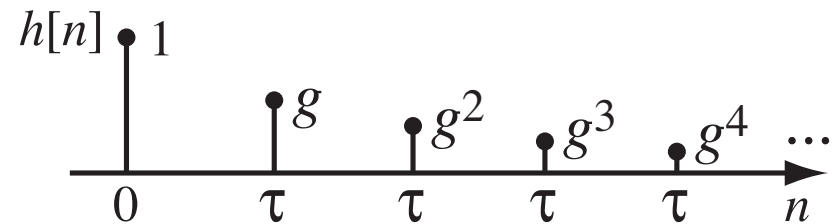
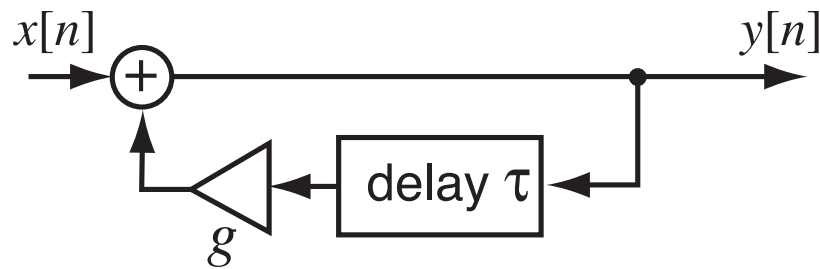


- **Range of perceptual effects**
  - $< 10$  ms - **phasing** (spectral structure)
  - 20-100 ms - **chorus/doubling**
  - $> 100$  ms - **echo**

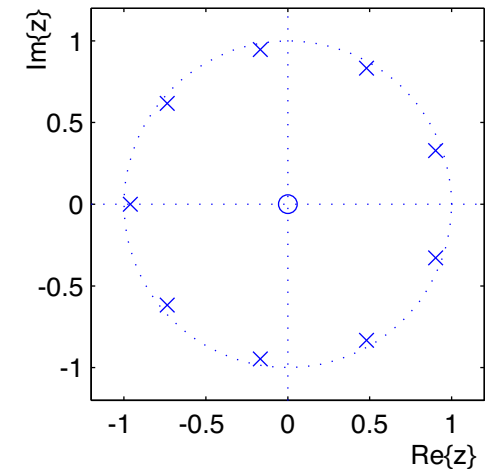
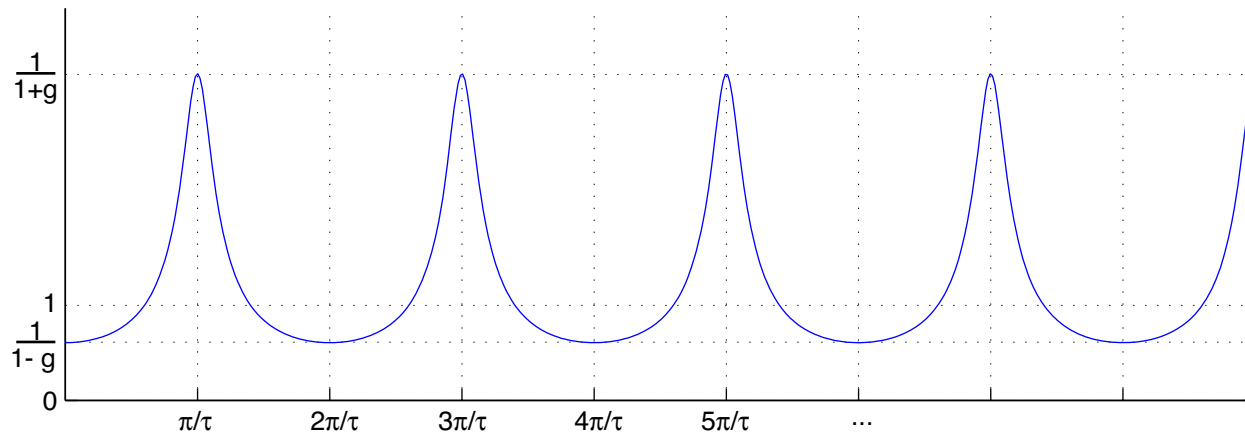


# IIR Comb Filters

- **Feedback delay** spreads out more in **time**

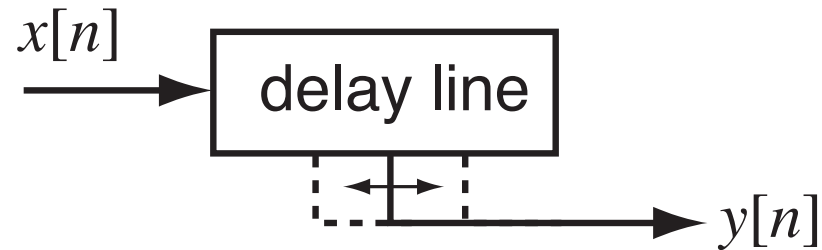


- Poles can give **unbounded** gain



# Time Varying Delay

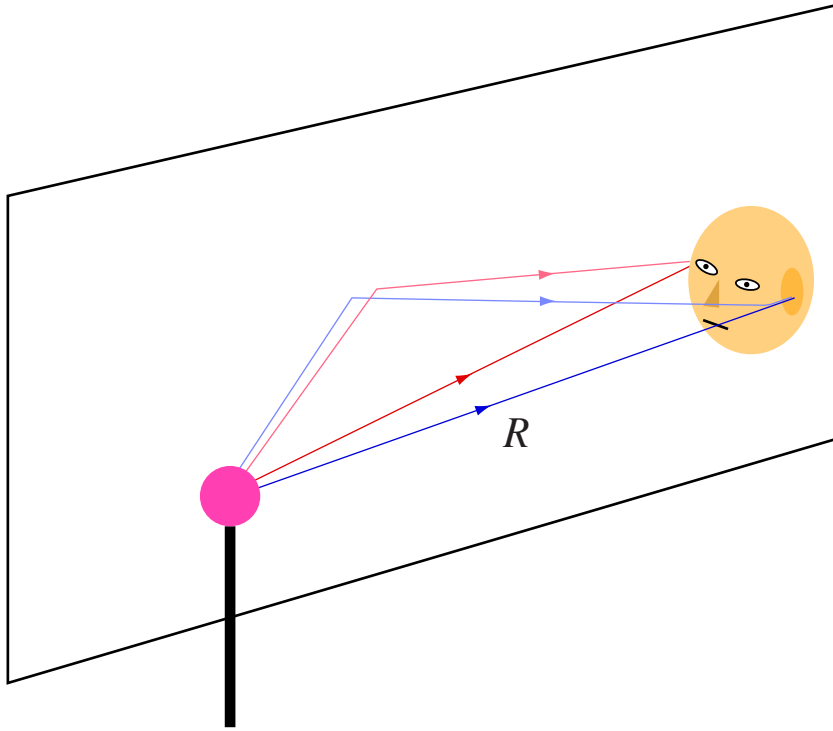
- Periodic variation over large range  
⇒ **Pitch modulation**
  - analogous to **Doppler** shift



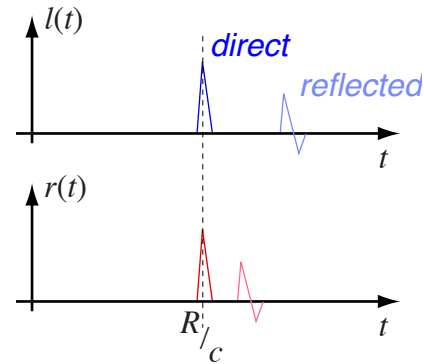
- Random (but smooth) shift over short delay  
⇒ **Chorus**
  - pattern of cancellation “notches” like detuned voices



# 3. Reverberation



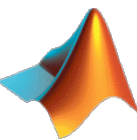
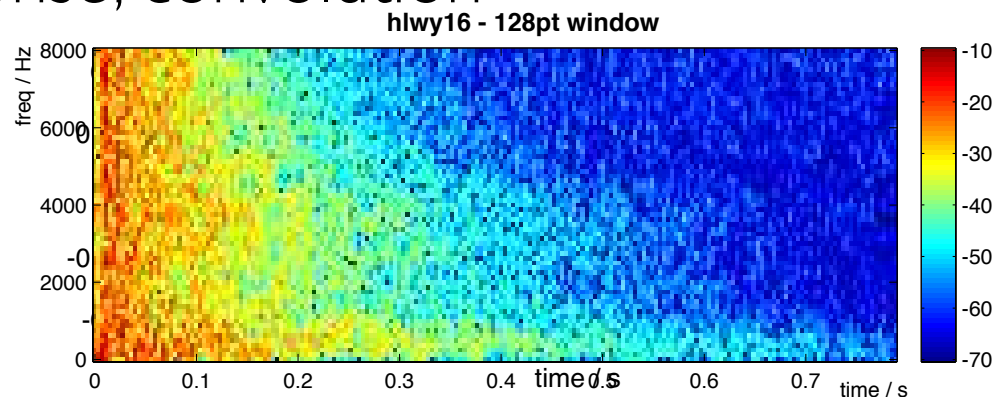
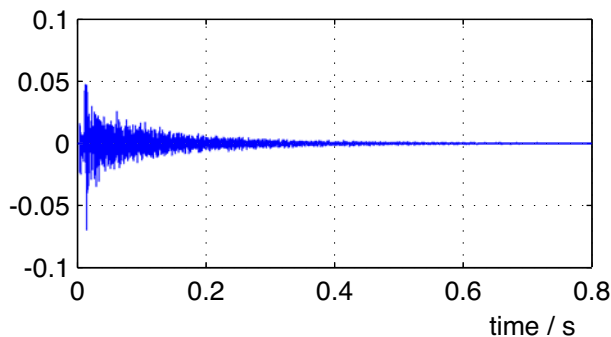
- Received sound is **direct path** + **reflections**



- delayed relative to direct path
- different at each ear
- Direct-to-Reverberant...

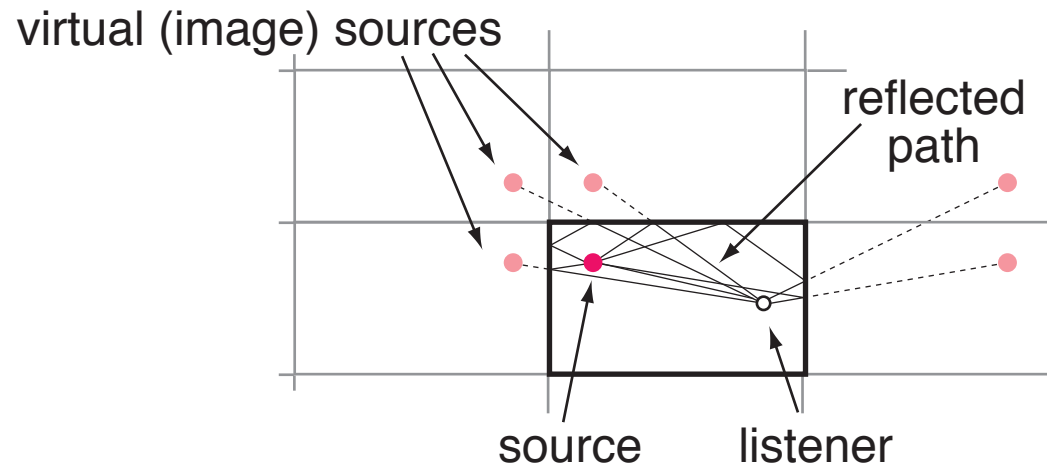
- Source  $\rightarrow$  Ear is  $\sim$  LTI

- can use impulse response, convolution



# Early Echoes & Late Reverb

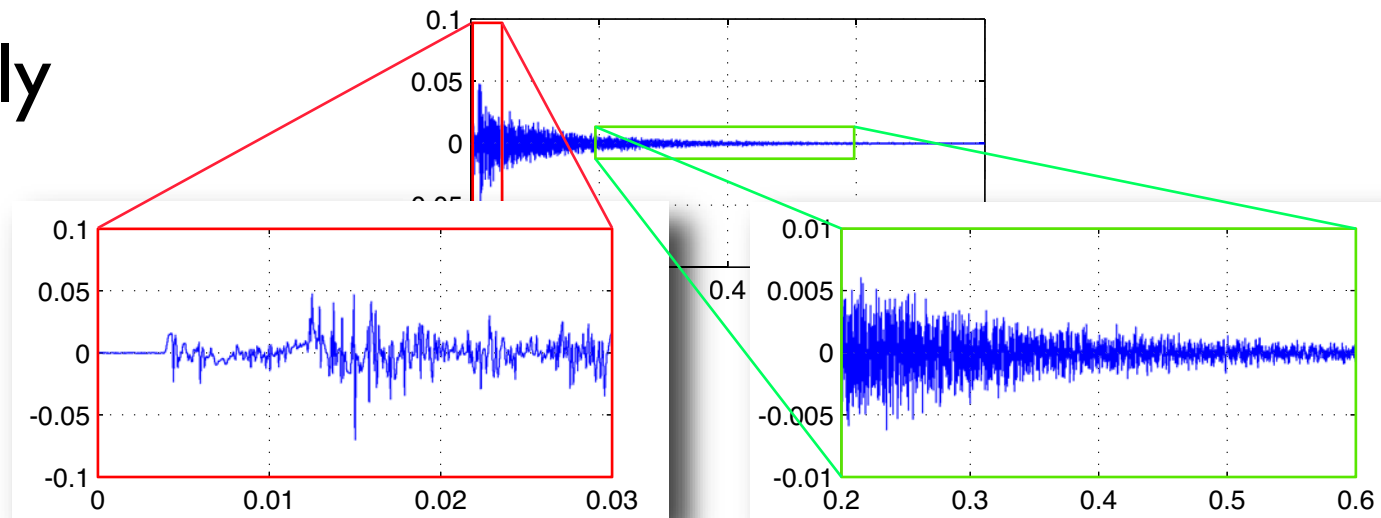
- Reflected paths are like “**virtual sources**”



- first part of reverberant IR is **sparse**

- Reflections quickly build up & **merge**

- later part of reverb is like **decaying noise**

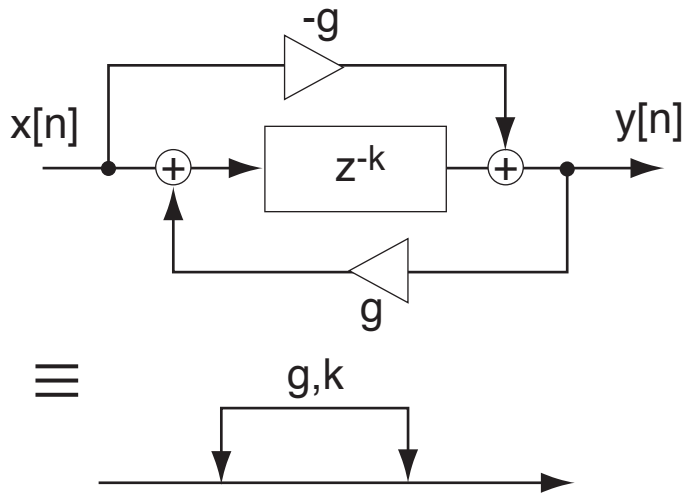




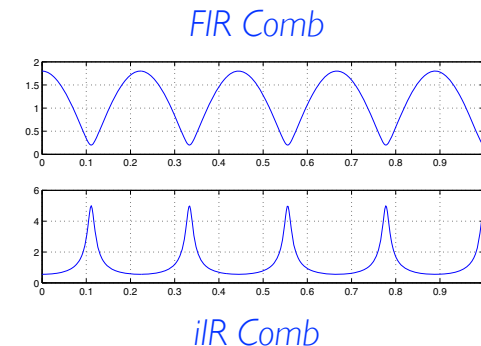
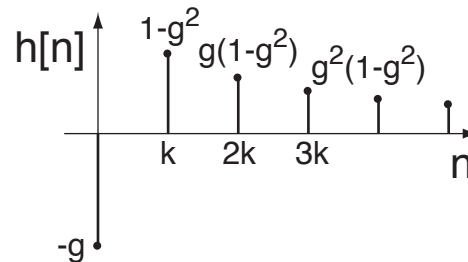
# Nested Allpass

- **Allpass** efficiently creates decaying response
  - multiple, combined filters for **complex** patterns

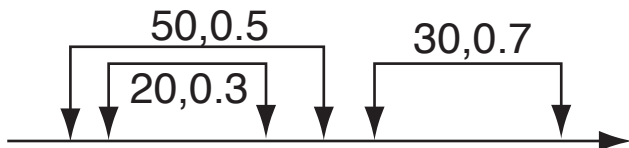
## Allpass



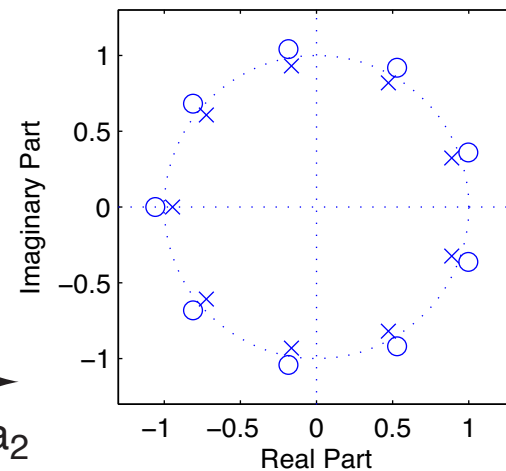
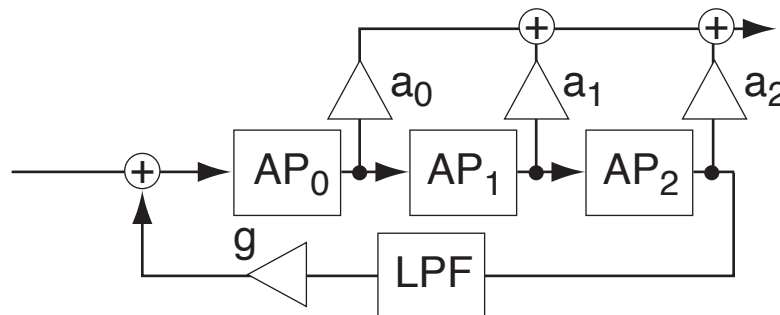
$$H(z) = \frac{z^{-k} - g}{1 - g \cdot z^{-k}}$$



## Nested+Cascade Allpass

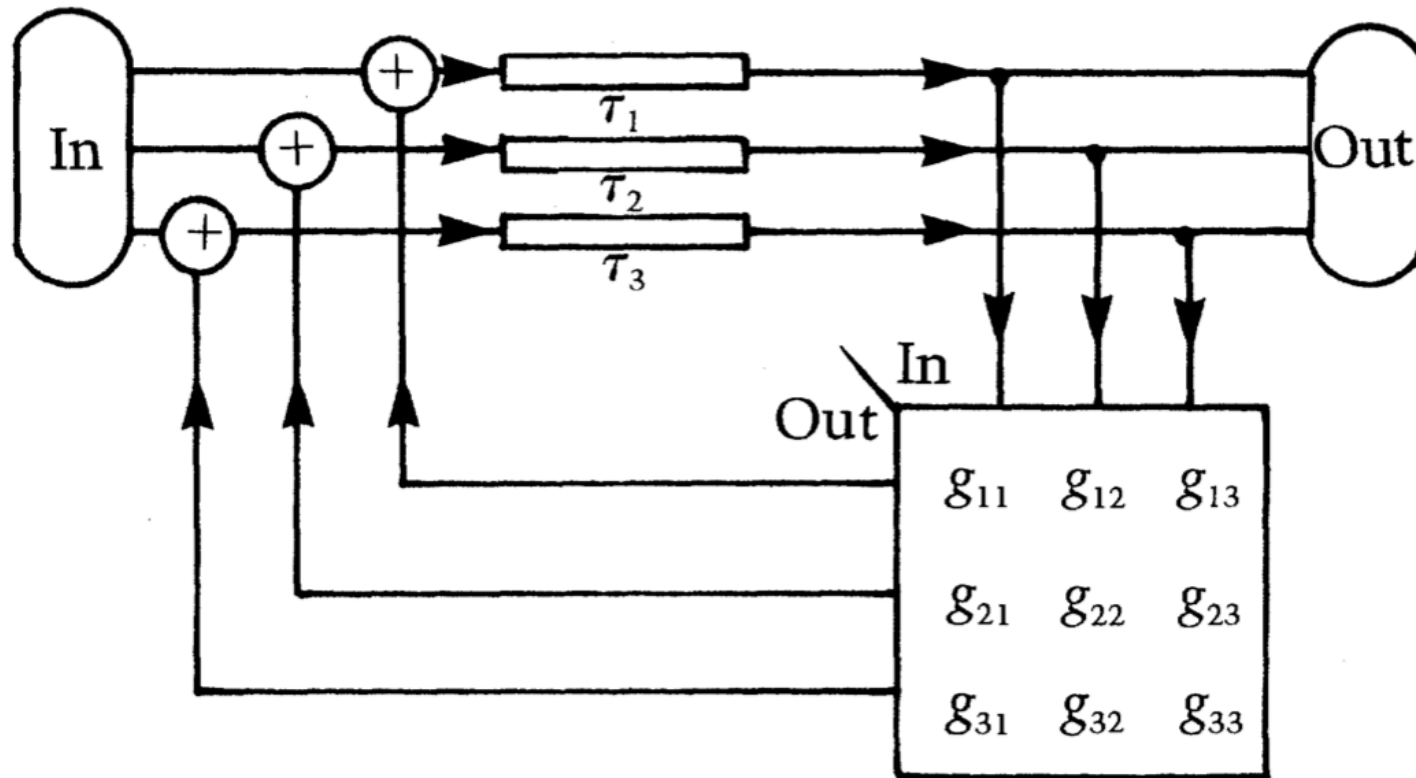


## Synthetic Reverb



# Feedback Delay Network

- **Matrix** of feedbacks gives even more complex patterns
  - “Unitary” matrix ensures decay



from Stauter & Puckette 1982



s16-reverb.pd

# Summary

- **Filters:**  
EQ used to balance mixes  
Varying filters gives effects e.g. Wah-wah
- **Delays**  
Wide range of effects: phasing ... echo  
Fractional delays
- **Reverb**  
Just a complex pattern of echoes  
Discrete early echoes → reverberant tail